

Using Hilbert Curves to Organize, Sample, and Sonify Solar Data

Abstract

How many ways can we explore the Sun? We have images in many wavelengths and squiggly lines of many parameters that we can use to characterize the Sun. We know that although the Sun is blindingly bright to the naked eye it **also** has regions that are dark in some wavelengths of light **and** bright in others. But both of those classifications are based on vision. Hearing is another sense that can be used to explore solar data. Some data, such as the sunspot number or the extreme ultraviolet spectral irradiance, can be readily sonified **by converting the data values to musical pitches**. Images are more difficult. **Using a raster scan algorithm to convert** a full-disk image of the Sun **to a stream of pixel values** is dominated by the pattern of moving on and off the limb of the Sun. A sonification of such a raster scan will contain discontinuities at the limbs that mask the information contained in the image. **As an alternative**, Hilbert curves are continuous space-filling curves that map a linear variable onto the two-dimensional coordinates of an image. We have investigated using Hilbert curves as a way to sample and analyze solar images. Reading the image along a Hilbert curve keeps most neighborhoods close together as the resolution (i.e., the order of the Hilbert curve) increases. It also removes most of the detector size periodicities and may reveal larger-scale features. We **present** several examples of sonified solar data, including the sunspot number, a selection of extreme ultraviolet (EUV) spectral irradiances, different ways to sonify an EUV image, and a series of EUV images during a filament eruption.

19 I. INTRODUCTION

20 **Sonifying a data set has the basic purposes of making data accessible to the blind and**
21 **allowing the data to serve as an adjunct to other senses. It can also help all to appreciate**
22 **or understand** a data set in a new way. Although a one-dimensional data set can be sonified by
23 scaling the data to pitches, image data is a more ambitious target. The data has variations in two
24 dimensions that should be represented by the sonification, and variations seen in a series of images
25 are even more difficult to sonify. Solar data is often in the form of images and the changes in time
26 and space are an integral part of understanding solar variations. We will describe sonifying several
27 solar datasets, including an exploration of ways to sonify solar images in space and time.

28 Composers have used many ways to create sounds and music that mimic the natural and me-
29 chanical worlds. Camille Saint-Saëns used pianos and other instruments to imitate about 14 an-
30 imals in *The Carnival of the Animals*.¹ Old-time fiddle tunes use the flexibility of the combined
31 performer and violin to imitate chickens and other natural sounds. Luigi Russolo built “intonaru-
32 mori” to produce a broad spectrum of modulated, rhythmic sounds that imitated machines.² He
33 also developed a graphical form of musical score to compose pieces for these devices. Others
34 have produced music from time sequences of the natural world. A well-known example is Concret
35 PH,³ which was created by splicing together short, random segments of tape recordings of burning
36 charcoal.

37 Analog electronic synthesizers provided another path. In their early stages they were often
38 used to produce sound effects. As analog synthesizers became more capable, such as the **Moog**
39 **modular synthesizer**,⁴ some used them to reproduce well-known musical pieces in electronic
40 form (e.g., *Switched-On Bach* by Wendy Carlos, 1968) while others invented new types of music
41 (the improvisations of Keith Emerson in the works of Emerson, Lake, and Palmer.)

42 Few, if any, of these techniques are examples of sonifying data. Sonification can be as simple
43 as the shrieking of a smoke alarm or as complicated as converting multi-dimensional data to an au-
44 dible signal. The incessant beeps and whistles of electronic vital sign monitors in hospitals are one
45 example where the change in a sound signals a change in health of the patient. These use the 1-D
46 structure of sound to convey information that conditions are both normal and alarming. **Whistlers**
47 **are an example of how scientists sonified radio frequency data to study the ionosphere.**⁵ The

48 **interactions of lightning with the electrons in the magnetosphere are heard as descending**
49 **tones lasting a few seconds.**

50 Digital electronic synthesizers give us the ability to convert any type of information from a
51 digital representation into music.⁶ **One example is that a** 1-D time series can be sonified by scaling
52 the values to musical pitches, assuming a constant duration for each value, to produce a set of
53 **Musical Instrument Digital Interface** (MIDI) commands. A MIDI-enabled synthesizer is then
54 used to create the musical instrument waveforms and play the commands in the MIDI file. Different
55 time series can be combined into a sonification by using different pitch ranges or timbres (the
56 distinctive set of tones in the selected instrument) to distinguish between them. We will use the
57 International Sunspot Number (Version 2, S) and extreme ultraviolet (EUV) spectral irradiances
58 from two satellites as examples of solar time series data.

59 Sonifying an image is different. Sound is intrinsically a 1-D format that evolves in time. A 2-D
60 image must be converted to a 1-D series of pixel values where the order of the pixels serves as the
61 time variable. Once the 1-D sequence exists, the pixel values are scaled to pitches, the duration is
62 again set to a constant, and the data run through the synthesizer.

63 There are many ways to map a 2-D image (or higher-dimensional data) to a 1-D sequence. A
64 raster scan is a linear reading of the image from the upper left to the lower right moving down to
65 the next row when the current one is read, much like reading an English language document. This
66 can be modified into a boustrophedonic algorithm where the first row is read left to right and the
67 next right to left, continuing in this way to the end of the image. This resembles the way an ox
68 (**Greek *bous***) plows a field and hence the term. Another way is to use a space-filling curve, such
69 as the Hilbert used here, to map the image pixels to a sequence. We will describe using Hilbert
70 curves to convert 2-D images into 1-D sequences and converting those sequences to sound.

71 The sonifications of these data sets will be described:

- 72 1. International Sunspot Number (annual and monthly variations)
- 73 2. Extreme ultraviolet (EUV) spectral irradiances as a time series and a spectrum
- 74 3. A complete EUV image and seven subimages
- 75 4. A montage of EUV images showing a filament liftoff

76 All of the sound files are available as .midi and .mp3 files at [https://sdo.gsfc.nasa.gov/sonify/](https://sdo.gsfc.nasa.gov/sonify/table.html)
77 table.html.

78 We start by introducing some useful musical concepts. That will be followed by a discussion
79 of the synthesizer used and the analysis of of the 1-D data sets. The image data will be introduced,
80 and an example using a raster scan to convert the data to 1-D will be described. We will then
81 describe the Hilbert curves used to address the image data and present several ways to sonify the
82 images. We discuss what can be learned from these sonifications and end with several conclusions
83 on the utility of this method. All of the science datasets are open-source and are available at the
84 locations listed in the Acknowledgements.

85 II. SONIFYING DATA

86 The JythonMusic software described in Manaris and Brown⁷ was used to convert a data series
87 into MIDI commands and drive a synthesizer. The concepts and terms we use to convert data to
88 music are:

- 89 • **Pitch:** One of 128 frequencies (spanning 10.75 octaves of the 12-tone equal-tempered scale),
90 from 8.18 Hz [C_{-1}] – 12.54 kHz [G_9]), with Middle C (C_4 , 261.63 Hz) roughly in the
91 middle at position 60. Twenty one pitches are added below the lowest note on the piano
92 and 19 pitches above the highest note. A range of only 128 values is small compared to the
93 linear range of many solar and geophysical data sets. It is also small compared to the pitch
94 discrimination of human ears. Untrained humans can discern pitch changes of $\approx 0.3\%$,⁸ so
95 roughly 43000 pitches would be necessary to resolve that frequency range. However, the
96 MIDI standard only allows limited microtones at that spacing. **Images encoded with the**
97 **Joint Photographic Experts Group (JPEG) algorithm** have pixel values ranging from 0–
98 255 (either in separate channels or through a color table), so we have only half of the range
99 in pitches. Transforming data **that varies by several orders of magnitude** into logarithms
100 **can compress** the range to small enough to sonify.
- 101 • **Duration and Tempo:** The **duration** (or length) of pitches and rests (periods of time without
102 any sound) are specified with a floating point number that can vary from 0 (no time) to 4
103 (corresponds to a whole note) and longer. **The tempo of a piece is the speed at which the**

104 **pitches and rests are heard.** Tempo is specified by the number of beats per minute (bpm);
105 where a quarter note (QN in JythonMusic) is one beat. **Durations** are relative to the tempo
106 of the piece, increasing the tempo proportionally reduces the duration of all pitches and rests.

- 107 • **Loudness:** The loudness (also called the dynamics or MIDI velocity) is set by an integer in
108 the range 0 (silent) to 127 (very, very loud). As the range of sound pressure level varies from
109 0 dB (threshold of hearing) to 120 dB (threshold of pain), the loudness maps to a change
110 of roughly one per dB. The response of human ears to loudness variations strongly varies
111 from one person to another and with frequency. The least noticeable change in loudness also
112 varies with frequency, but a reasonable value is 0.4 dB.⁹ This corresponds to a 5% change in
113 pressure and is easily accommodated by the 128 possible values. We only use loudness to
114 weight the various datasets. It is also possible to encode information in the loudness, such
115 as a longer duration being louder, but we do not present such cases here.
- 116 • **Timbre:** There are 128 possible timbres in the MIDI standard. These timbres are not specified
117 in the MIDI standard and a numbered timbre may sound different in different synthesizers.
118 One channel is devoted to percussion and uses the pitch designator to select a percussive
119 timbre.
- 120 • **Pan:** Position in space is limited in this study to left-right pan. A floating point number
121 between 0 (left) and 1 (right) determines the position, with 0.5 (centered) the default. Placing
122 one data set in the left side and another in the right is a good way to compare two data sets.
123 Where they agree the sounds will appear to come from the middle and otherwise they will
124 come from separate sides.

125 JythonMusic is based on Java rather than C. Programs in JythonMusic are written in Python 2.7
126 syntax but do not have access to many of the libraries used for numerical work. **As a result,** data
127 access and extraction routines were written and executed in a C-based Python environment that
128 provided access to the NumPy library for array manipulation. The computational sequence was to
129 read the data, extract the appropriate part, write the extracted data to a **comma-separated variable**
130 (CSV) file, read that file in the JythonMusic environment, convert the data into a MIDI file, and use
131 the JythonMusic synthesizer to play that file. **A permanent record was created by playing the**
132 **MIDI commands in another synthesizer that could export the sounds to an MP3 file.**

133 III. SAMPLING AND SONIFYING SOLAR DATA

134 Several types of solar data were sonified and reported here. A summary is presented in Table I,
 135 where the source, type, and name of **the corresponding** MP3 file are listed. The Sec. column is
 136 the part of the paper where the data is described. A version of this table, with links to the MP3 and
 137 MIDI files, is available at <https://sdo.gsfc.nasa.gov/sonify/table.html>.

TABLE I. Files for each Sonified Data Set

Sec.	Source	Sonified Data	mp3 Filename
III A	SIDC	Sunspot number	TS_sunspot_annual_month.mp3
III B	EVE	EUV spectral irradiances (spectrum)	TS_EVE_sonified.mp3
III B	SEE	EUV spectral irradiances (time series)	TS_SEE_sonified.mp3
III C	AIA 193 Å	Complete image (raster)	AIA_193_full_image_sonified_raster.mp3
V	AIA 193 Å	Complete image (Hilbert)	AIA_193_full_image_sonified.mp3
V A	AIA 193 Å	Subimage 1 (Arcs)	subimage_1_x_685_y_1755.mp3
V A	AIA 193 Å	Subimage 2 (Fan)	subimage_2_x_1060_y_1120.mp3
V A	AIA 193 Å	Subimage 3 (Island)	subimage_3_x_1290_y_1690.mp3
V A	AIA 193 Å	Subimage 4 (Limb)	subimage_4_x_1800_y_992.mp3
V A	AIA 193 Å	Subimage 5 (Spot)	subimage_5_x_890_y_1035.mp3
V A	AIA 193 Å	Subimage 6 (Swirl)	subimage_6_x_750_y_1125.mp3
V A	AIA 193 Å	Subimage 7 (X)	subimage_7_x_760_y_405.mp3
V B	AIA 193 Å	Filament liftoff montage	liftoff_complete.mp3

139

140

141 A. International Sunspot Number

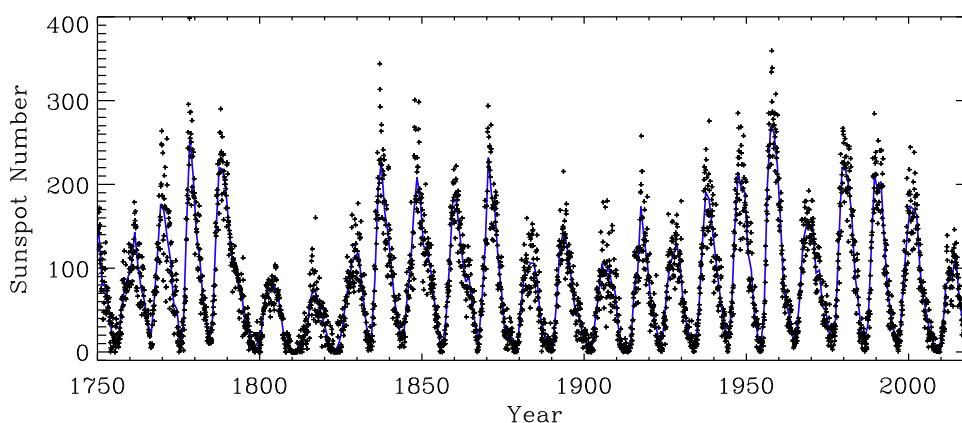
142 The first example is the variation of the International Sunspot Number (S) with time. The
 143 sunspot number is a weighted count of dark regions on the Sun that is often used as a long-term
 144 index of solar activity. It has been measured or derived for roughly 400 years. It is the source of
 145 much of our knowledge of the evolution of solar activity. We use Version 2 of the International
 146 Sunspot Number^{10,11} between 01 Jan 1750 and 31 Dec 2018 from the Solar Influences Data analysis

147 Center (SIDC) website, both the monthly and annually averaged values. The time dependence of
 148 S is shown in Figure 1.

149 After some experimentation, we determined the following sonification. The annually-averaged
 150 values were mapped to pitches between 48 and 96 of the lower timbre (PICKED_BASS) and a
 151 loudness of 125. This data was used to set the tempo (one year is one beat with a duration of a
 152 quarter note) of 400 bpm. The monthly-averaged values were mapped to pitches between 60 and
 153 108 in the PIANO timbre and a loudness of 100. This data is played at 12 values per beat, and was
 154 panned left-right with a two-year period. This allows you to hear the differences in the two signals.
 155 The slower lower voice can be audibly distinguished from the more rapidly varying higher voice.

156 You can listen to this sonification at

157 https://sdo.gsfc.nasa.gov/iposter/mp3/TS_sunspot_annual_month.mid.mp3



158

159 FIG. 1. Version 2 of the International Sunspot Number as a function of time since 1750. The solid blue line
 160 is the annually-averaged data (plotted at the middle of each year) and the '+' symbols show the monthly-
 161 averaged values.

162 B. Extreme Ultraviolet Spectral Irradiances

163 The next example is to sonify extreme ultraviolet (EUV) spectral irradiances from two instru-
 164 ments in two ways. The solar EUV spectral irradiance spans wavelengths between X-rays and the
 165 ultraviolet (roughly 10–100 nm) but is often extended to include the H I 1216 emission line (Ly-

166 α). (Emission lines are described by the element symbol, the ion state of the element [where
167 H I is neutral hydrogen, H II is singly-ionized hydrogen, etc.], and the wavelength of the line
168 in Å.) This radiation is easily absorbed as it ionizes the outer electrons of many elements. This
169 also makes it the major source of the ionosphere in the terrestrial and planetary atmospheres. The
170 EUV emissions are also a direct measure of the magnetic field. The Sun would have considerably
171 smaller EUV emissions if it did not have a magnetic field. The **ratio of the spectral irradiance**
172 **at the EUV wavelength of 30.4 nm to the peak value of a 5770 K blackbody at a visible wave-**
173 **length of 500 nm** is 10^{-26} . This ratio is 10^{-4} in a solar spectrum. These two properties, sensitivity
174 to the solar magnetic field and acting as the source of the ionosphere, make measurements of the
175 solar EUV spectral irradiance a primary goal in solar physics.

176 **Solar EUV spectral irradiances are completely absorbed by the atmosphere and must be**
177 **measured by an instrument in space. These instruments record the spectral irradiances as a**
178 **function of wavelength and time. We first sonify a single spectrum** from the Extreme ultraviolet
179 Variability Experiment (EVE)¹² on NASA's Solar Dynamics Observatory (SDO).¹³ EVE data is
180 available from 5 to 105 nm from 1 May 2010 until 26 May 2014 and from 37–105 nm thereafter.
181 **Figure 2 shows that the EUV spectral irradiance has many emission lines, two of the strongest**
182 **(He I 304 and C III 977) are labeled, and several roughly triangular regions of continuum**
183 **emission (such as the one highlighted between 70 nm and 91 nm.) The third label points to**
184 **the emission line Fe XII 193, which will be explored in later sections.**

185 We elected to sonify the day-averaged solar EUV spectrum from EVE on 27 Feb 2014, the day
186 of maximum sunspot number for Solar Cycle 24 (Figure 2). The log of the spectral irradiances was
188 scaled to MIDI frequencies 36–96. That means every order of magnitude in the data spans about
189 1.5 octaves. The PIANO timbre was used, the tempo was set to 600 bpm, and the loudness was set
190 to 80.

191 This example shows how the independent variable, in this case wavelength, does not have to be
192 time to sonify a data set. **The independent variable must at least provide an ordering of the**
193 **data set, in this case with a uniform spacing between the data points.** This was the judged to be
194 the most musical example. **Some of Bach's Goldberg Variations (BWV 988) sound much like**
195 **this sonification. One part, at around the 33-minute mark as played by Glenn Gould in his**
196 **1981 album of the same name, has a long chromatic run that sounds like gradual rise of the**

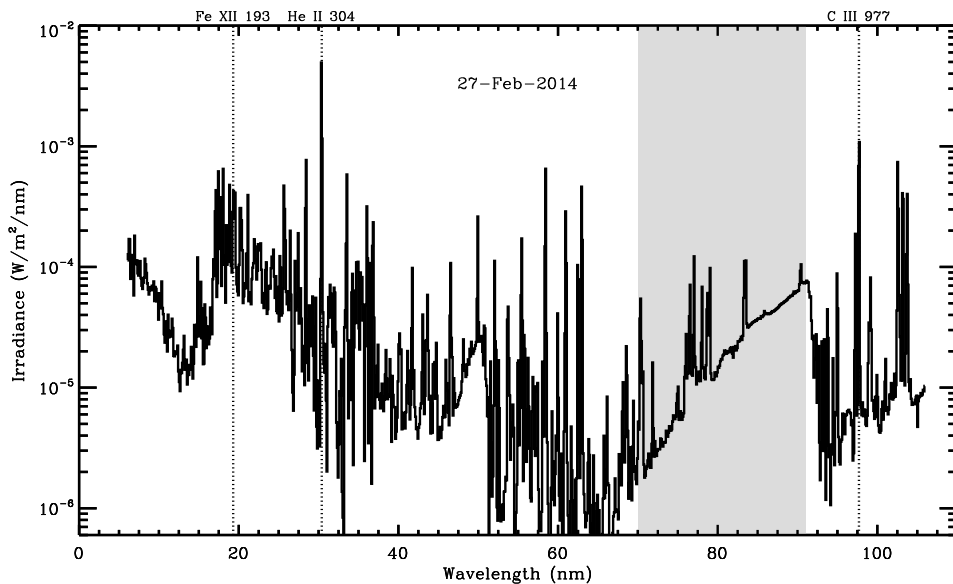


FIG. 2. A day-averaged EUV spectral irradiance for 27 Feb 2014, as measured by EVE, plotted against the wavelength in nm. The seven AIA passbands are identified with vertical dashed lines. The He II 304 Å line is the brightest in this wavelength range, with the C III 977 Å line the next brightest. **The 70–90 nm continuum emission region is highlighted. The Fe XII 193 emission line will be analyzed in images below.** Although the total radiant energy in this spectrum is 4.7 mW m^{-2} , about 10^{-5} times the total solar irradiance of 1361 W m^{-2} , it is responsible for much of the ionization in the thermospheres of the Earth, Venus, and Mars.

197 **EUV spectrum between 70–91 nm. The rapid increases in pitch of the strong spectral lines**
 198 **also add musical contrast to this piece.**

199 You can listen to this sonification at

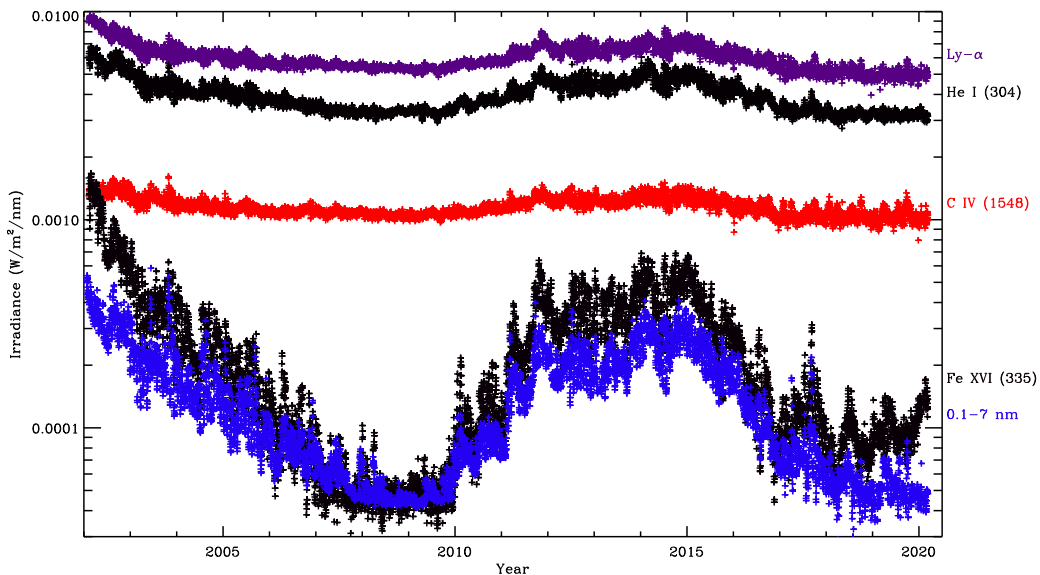
200 https://sdo.gsfc.nasa.gov/iposter/mp3/TS_EVE_sonified.mid.mp3

201 **Spectral irradiances at selected wavelengths can also be extracted from the measurements**
 202 **as a function of time.** The longest source of EUV spectral irradiances is the Solar Extreme ul-
 203 traviolet Experiment (SEE)¹⁴ on NASA’s Thermosphere Ionosphere Mesosphere Energetics and
 204 Dynamics (TIMED) spacecraft. The spectral irradiances from 9 Feb 2002 to 11 May 2019 of sev-
 205 eral strong emission lines (He I 304, Ly- α , C IV 1548, and Fe XVI 335), along with the 0.1–7 nm
 206 soft X-ray radiometer channel, were sonified. The time dependence of these channels is shown in

207 Figure 3. Pitches between 24 and 108 were interpolated from the log of the irradiances using the
 208 maximum and minimum of each channel as the limits. This forces the channels to have the same
 209 pitch range. The timbres were PIANO, PICKED_BASS, TROMBONE, FLUTE, and MARIMBA,
 210 respectively. The tempo was set to 640 bpm and the loudness was set to 100.

211 You can listen to this sonification at

212 https://sdo.gsfc.nasa.gov/iposter/mp3/TS_SEE_sonified.mid.mp3



213

214 FIG. 3. The variation of selected EUV spectral irradiances from SEE with time. The selected wavelengths
 215 show different levels of solar cycle modulation. The Ly- α and 0.1–7 nm irradiances were divided by 10 and
 216 20, respectively, before plotting.

217 C. Extreme Ultraviolet Images

218 Although measuring the EUV spectral irradiance is important, understanding those emissions
 219 requires that you also have images at those wavelengths showing how the source regions of the
 220 emissions vary in both space and time. Extreme ultraviolet images from the Atmospheric Imaging
 221 Assembly (AIA)¹⁵ on SDO were sonified as complete images, subimages, and a time sequence
 222 of subimages. AIA provides 10 passbands: seven EUV, two ultraviolet, and one visible light.
 223 AIA 193 Å images were selected as they highlighted the desired coronal details. We will describe

224 different ways to sonify an AIA image from 18 Mar 2018 (20190318_235553_2048_0193.jpg).

225 **Compared with time series data, we found that** images are difficult to sonify because they
 226 are dense in information **and have variations in two directions**. As an example of density, a
 227 sonified 512×512 image would take almost 15 hours to listen to at a moderate tempo of 300 bpm,
 228 and a full-resolution (4096×4096) AIA image would require 40 days. Many people have a hard
 229 time remembering tone sequences and whatever is happening near the end would be disconnected
 230 from the beginning. We overcome this by either binning the image to a smaller number of pixels
 231 or selecting subimages. **Based on our experiences when playing our sonifications, where we**
 232 **found that** a person can remember tone sequences for a few minutes, we aim to create sonifications
 233 that last three minutes by binning the image to 32×32 pixels or by using much higher tempos (up
 234 to 3000 bpm). Pieces such as John Cage's *Organ²/ASLSP (As Slow as Possible)* may be written
 235 for performance times of hours to years, but the density of notes is far smaller in these pieces.
 236 Only 29 notes have been sounded since a 639 year version of the piece was begun in 2001 at the
 237 **Burchardikirche in Halberstadt, Germany**.¹⁶ An AIA image would sound 29 notes in the first
 238 5.8 s at our standard tempo of 300 bpm.

239 AIA science data is served as monochromatic, $4k \times 4k$, 14 bit files using the Flexible Image
 240 Transport System (FITS).¹⁷ **To make these sonifications more accessible to students, we elected**
 241 **to use the** quicklook AIA images that are served as JPEG files created from the FITS data using
 242 log scaling and an arbitrary color table. **Concentrating on converting JPEG images allowed**
 243 **us to test the algorithms using images with higher contrast features**. The JPEG images were
 244 converted to greyscale using the luminosity form **of relative luminance** to weight the individual
 245 red (R), green (G), and blue (B) channels:

$$IM(B\&W) = 0.21R + 0.72G + 0.07B, \quad (1)$$

246 but starting from the original FITS files would produce very similar results once a logarithmic scal-
 247 ing was applied. **Although the solar images used have redundant information in the separate**
 248 **color channels**, by applying the luminosity form to all JPEG images it is possible to analyze any
 249 image with a three-color format. The greyscale images are then sampled along a **raster scan** as de-
 250 scribed above. One initial image is shown in Figure 4, with the left image overdrawn with a raster
 251 scan and the right image overdrawn with a Hilbert curve, which will be described in Section IV
 252 below.

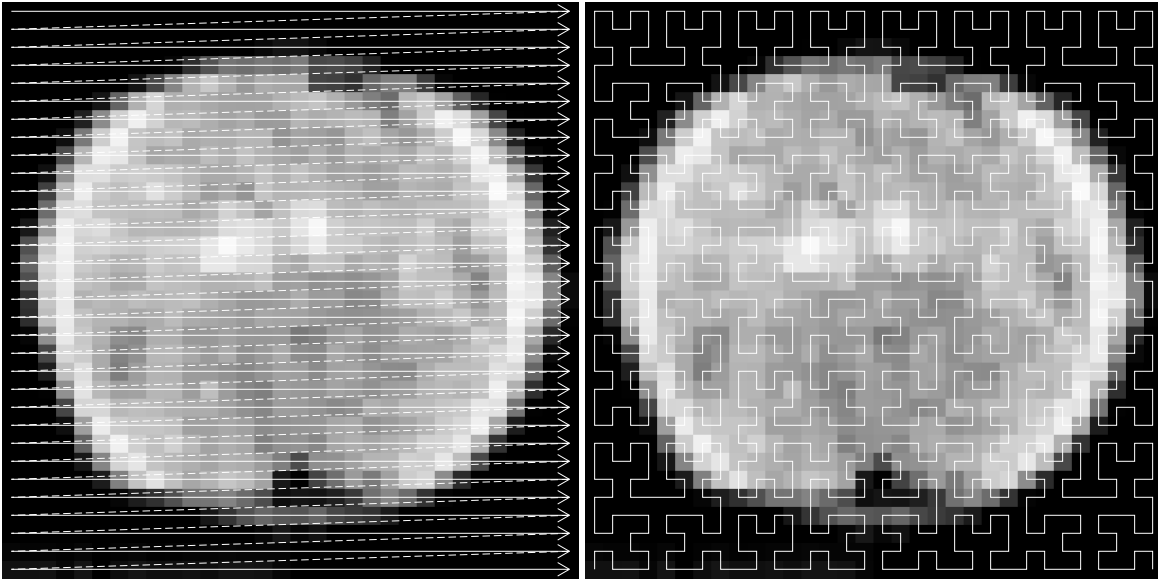


FIG. 4. A greyscale SDO/AIA 193 Å image from 18 Mar 2019 binned from 2048×2048 to 32×32 . On the left is an example of how a raster scan from the top left to the lower right samples the image. The dashed lines are the return from right to left that is not used in the sampling. In the right panel an $n = 5$ Hilbert curve (H_5) is drawn over the image. Each pixel in the image is assigned to a point in the curve. The centers of square pixels are located where the curve has a right angle bend, at the halfway mark of straight segments that are two units long, or two centers proportionally spaced along the straight segments that are three units long.

253 The image was sampled in two different resolutions. The higher register (pitches 60–120) was
 254 scaled from the 32×32 binned image and assigned the SOPRANO_SAX timbre. The lower
 255 register (pitches 48–96) was scaled from a 16×16 binned image resampled to 32×32 so that both
 256 registers have the same number of pulses and assigned the ACOUSTIC_GRAND timbre. The dark
 257 regions of the lower register were omitted by being set to the special variable REST.

258 You can listen to this sonification at

259 https://sdo.gsfc.nasa.gov/iposter/mp3/AIA_193_full_image_sonified_raster.mp3

260 The upper curve (a) in Figure 5 shows how the raster scan is dominated by the quasi-periodic
 261 variations caused by the scan moving onto and off of the disk of the Sun. As a result, we explored
 262 using other methods to sample the image. The Hilbert curve was one of those methods.

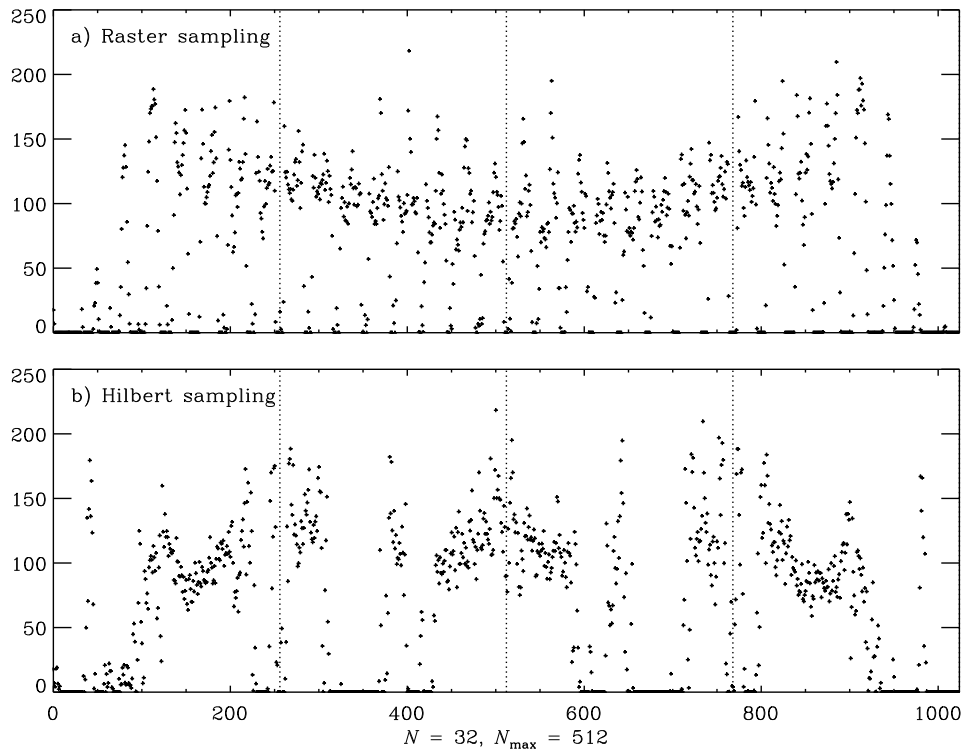


FIG. 5. Sampling curves for the AIA 193 Å image in Figure 4 binned to 32×32 . The top plot (a) used a raster scan to sample the pixels (the left panel in Figure 4.) The lower plot (b) used a Hilbert curve to address the image (the left panel in Figure 4.) The vertical lines show the four horizontal strips of (a) and the quadrants of (b).

263 IV. HILBERT CURVES

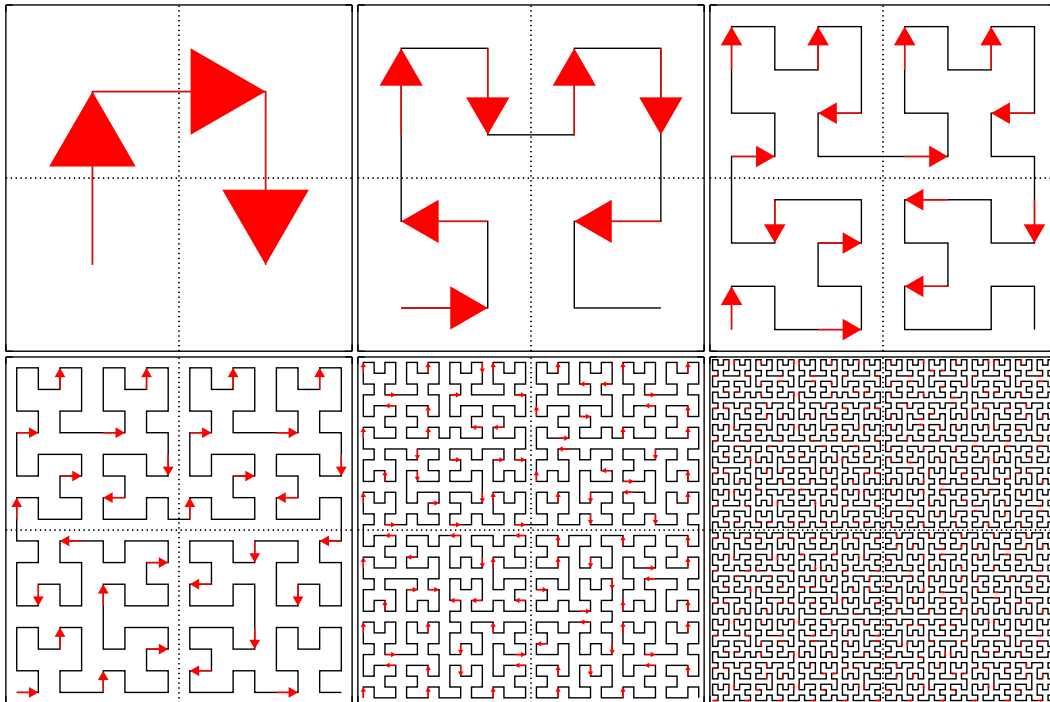
264 Hilbert curves are continuous space-filling curves that have been used in a surprisingly large
 265 number of disciplines. They were first described by Hilbert¹⁸ as a simpler form of the space-filling
 266 curves of Peano¹⁹. A true Hilbert curve exists only as the limit of $n \rightarrow \infty$ of the n^{th} approximation
 267 to a Hilbert curve (H_n). However, the approximations are useful to provide mappings of 2-D
 268 images onto a 1-D sequence. Figure 6 shows H_n for $n = 1, 2, \dots, 6$.

269 A summary of **the** properties of H_n :

270 1. There are 2^n pixels along each side of the square containing the curve

271 2. The Euclidean length of H_n grows exponentially with n , $2^n - 2^{-n}$

- 272 3. H_n covers a finite area as it is always bounded by the unit square
- 273 4. Two points in the image, (x_1, y_2) and (x_2, y_2) , that are close together in H_n are also, with a
- 274 few exceptions, close together in $H_{n'}$, $n' > n$



275

276 FIG. 6. The first six Hilbert curves, plotted from upper left to lower right, with arrows showing the direction

277 of the motion into each vertex. Each subplot is drawn with axes limits of $[0,1]$ in both directions. Among

278 the most important properties of these curves is the single line connecting two quadrants. This can be seen

279 by examining the dotted lines drawn to separate the quadrants. Another property is that the sampling goes

280 around each quadrant in a similar motion (upper quadrants are sampled in a clockwise fashion and the lower

281 quadrants in a counter-clockwise fashion.)

282 A Hilbert curve maps a linear variable onto the two-dimensional coordinates of an image. Its

283 inverse is a mapping of the image coordinates onto a linear variable. This mapping property means

284 we can use Hilbert curves to map solar images onto a linear sequence of pixel values that can then

285 be sonified. Images tend to have dimensions that are powers of 2, so the Hilbert curves are a natural

286 fit to addressing them.

287 Reading the image along a Hilbert curve has the advantage of keeping neighborhoods close to-
 288 gether as the resolution (i.e., the length of the curve) increases. It also removes most of the detec-
 289 tor size periodicities and actually shows the presence of longer-scale features. Because successive
 290 H_n 's pass through similar neighborhoods as the resolution is refined, Hilbert curve samplings can
 291 be overplotted in time to provide contrasting versions of the image.

292 The neighborhood property works with other space-filling curves. Bartholdi et al.²⁰ describe
 293 using a Sierpinski space-filling curve to design delivery routes for Meals on Wheels. The system
 294 was simple, cheap, and paper-based. It used a manual "Rolodex" method of entering or removing
 295 addresses.

296 Vinoy et al.²¹ and others have shown how to use Hilbert curves to construct microwave an-
 297 tennas. They used models and measurements of the input impedance to show that a small square
 298 overlain with a conducting Hilbert curve produced an antenna whose resonance frequencies were
 299 consistent with a much longer wire antenna. They also showed how those frequencies shifted and
 300 how additional resonances were added as the order of the Hilbert curve was increased. This makes
 301 these antennas useful for mobile wireless devices.

302 Seeger and Widmayer²² describe using space-filling curves to access multi-dimensional datasets
 303 with a 1-D addressing scheme. The 1-D curve imposes an order on the data access that is diffi-
 304 cult to implement using a multi-dimensional access polynomial. **Morton²³ describes using the**
 305 **space-filling Z-order curves to access a file address database. Like the Hilbert curve, Z-order**
 306 **curves preserve the locality of most of the points being mapped.**

307 Multi-dimensional Fourier integrals (as well as others) can be reduced to a 1-D form by map-
 308 ping the coordinates onto a space-filling curve, essentially converting the integral into a Lebesque
 309 integral.²⁴

310 V. EXTREME ULTRAVIOLET IMAGES SAMPLED ALONG HILBERT CURVES

311 The difference between the sampling along a Hilbert curve and a raster scan can be seen in
 312 Figure 5, where the sampling curves for the image in Figure 4 (binned to 32×32) are shown. The
 313 bottom curve (b) in Figure 5 shows how the Hilbert curve sampling localizes the off-disk portions
 314 of the image along the curve and hence in time in the sonified version.

315 The pixels in the raster scan sonification were converted to tones by mapping pixels values
 316 between [0,250] to pitches [60, 120] (or C4 to C9, a span of 5 octaves). The duration was set to a
 317 sixteenth note, the loudness to 110, and the PIANO timbre was used. In the Hilbert curve sampling
 318 the 32×32 pixels were sonified with the same values except the SOPRANO_SAX timbre was
 319 used. A second voice was added mapping pixels values between [0,250] to pitches [48, 96] (or
 320 C3 to C7, a span of 4 octaves). The duration was set to a quarter note, the loudness to 90, and the
 321 ACOUSTIC_GRAND timbre was used.

322 You can listen to this sonification at
 323 https://sdo.gsfc.nasa.gov/iposter/mp3/whole_AIA_193_full_image_sonified.mid.mp3

324 **A. Using Subimages to Emphasize Features in Extreme Ultraviolet Images**

325 The AIA 193 Å image in Figure 5 is vastly undersampled. The length of an image sonification
 326 scales as n^2 , where n is the order of the Hilbert curve. One way to increase the accuracy of the
 327 sampling while keeping a reasonable length in the sonification is to sub-sample the image. Seven
 328 64×64 subimages of the 2019 Mar 18 image are shown in Figure 7, numbered to agree with
 329 Table I.

331 The duration was set to a sixteenth note, the tempo to 300 bpm, the loudness to 110, and the
 332 PIANO timbre was used. Each subimage was sampled along a Hilbert curve. The full-resolution
 333 pixels were sonified with the same values as the full image Hilbert curve sampling example above
 334 with the exception that the range of pixel values was [0, 255]. A second voice was added mapping
 335 pixels values between [0,255] to pitches [48, 84] (or C3 to C6, a span of 3 octaves). The duration
 336 was set to a quarter note, the loudness to 75, and the ACOUSTIC_GRAND timbre was used.

337 You can listen to this sonifications by accessing the clickable image at
 338 <https://sdo.gsfc.nasa.gov/iposter/>.

339 **B. Filament Liftoff Sequence in Extreme Ultraviolet Images**

340 The final example is sonifying a series of images from AIA on SDO. We selected the filament
 341 liftoff of 2010 Mar 10–12 as **an** example (**Figure 8**). Eight subimages were extracted that included
 342 the filament liftoff and the lower-left and upper-left quadrants of those subimages were sampled

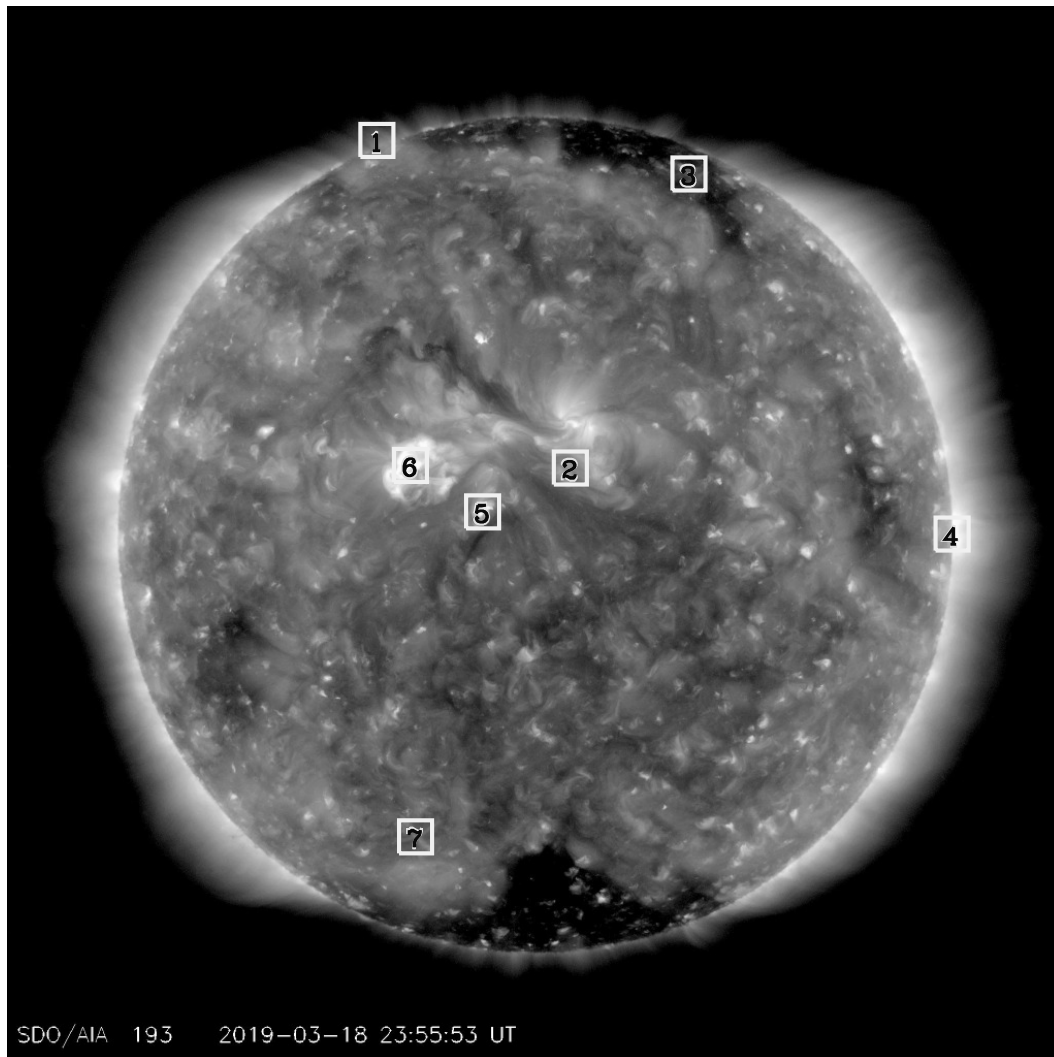


FIG. 7. A greyscale SDO/AIA 193 Å image from 18 Mar 2019. This image will be used as an example for sonifying still images. The boxes mark the locations of the examples in Table I.

343 along a Hilbert curve and sonified. A short chorus and ending cadence were written. The piece
 344 was made by inserting the subimages in turn, separated by a chorus and ending with the cadence,
 345 thus creating a single time series of pitches.

346 The pixels in this sequence were converted to tones by subtracting the average of each image
 347 from the sampled data, mapping the resultant values from $[-60, 60]$ to pitches $[36, 96]$ (or C2 to
 348 C7, a span of 5 octaves). The duration was set to a sixteenth note, the loudness to 110, and the
 349 PIANO timbre was used.

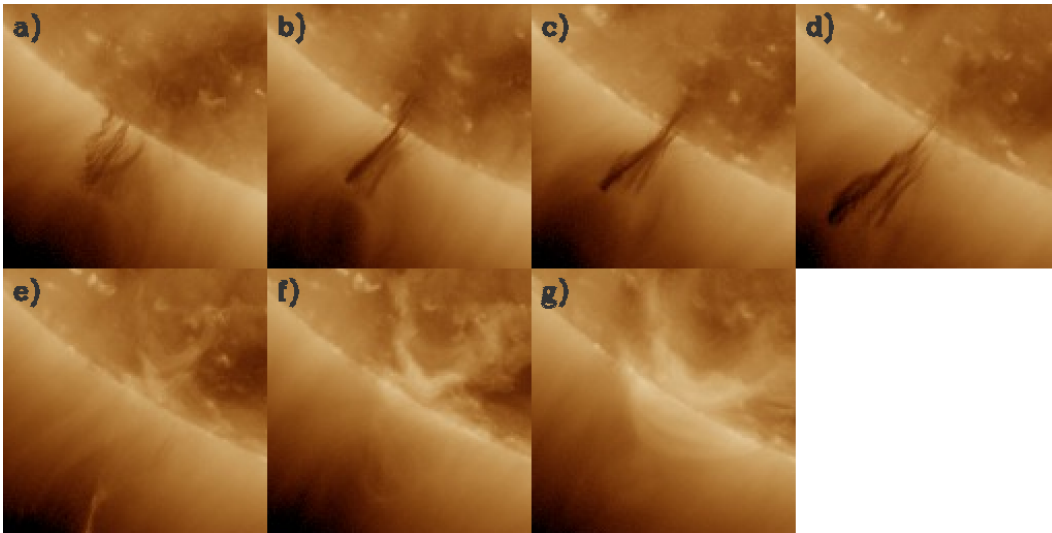


FIG. 8. Montage of seven solar images showing a filament liftoff. **Starting from the upper left, the images were recorded at a) 2012-03-10 02:27:20 UTC, b) 2012-03-11 03:27:44 UTC, c) 2012-03-11 17:59:08 UTC, d) 2012-03-11 23:29:08 UTC, e) 2012-03-12 01:29:20 UTC, f) 2012-03-12 02:28:56 UTC, g) 2012-03-12 04:27:56 UTC, and h) 2012-03-12 06:29:56 UTC, respectively.**

350 You can listen to this sonification at
 351 https://sdo.gsfc.nasa.gov/iposter/mp3/liftoff_complete.mid.mp3

352 This was the least satisfying sonification because the changes in time were subtle and difficult
 353 to resolve. We have been investigating other ways to show the movement of material through both
 354 space and time. The subtraction of the mean was example of one such technique. By removing the
 355 average any overall brightening or darkening of the region did not dominate the change in time.

356 VI. DISCUSSION OF SONIFIED DATA

357 Based on our experiments, percussive sounds, such as PIANO and PICKED_BASS, seem to
 358 work better for sonifying data. Percussive timbres securely place the sound on the beat and produce
 359 interesting changes as the tempo increases. A timbre with a noticeable rise or decay time tends to
 360 sound muddy as the tempo is increased.

361 Our attempts to create a beat and melody by playing two versions of averaged data, such as the
 362 annual vs. the monthly values of S , were not a complete success. We continue to explore how to

363 make the sonified data more like music and less mechanical.

364 Although sonified data does not sound like most types of music, at least some pieces of classical
365 music has similar qualities. Bach's Goldberg Variations (BWV 988) sounds much like the image
366 sonifications described above. As we note above, at around the 33-minute mark as played by Glenn
367 Gould in his 1981 album of the same name, the long chromatic run sounds quite similar to the EVE
368 spectrum.

369 You cannot create an MP3 file directly from the JythonMusic synthesizer. You can capture
370 the sounds in **either a recorder or software such as Audacity while** the MIDI commands are
371 executed. Or you can load the file containing the commands into another synthesizer. The MP3
372 files listed here were created by playing the MIDI files in GarageBand, a proprietary program from
373 Apple, **although any suitable synthesizer could be used.** You can also change the timbre of a part
374 in GarageBand, providing another level of experimentation. Different synthesizers assign different
375 timbres to each instrument channel, so the listed MP3 files do not always match what is heard when
376 the JythonMusic synthesizer is used. Other timbre files can also be used with the synthesizers.

377 You can also use other programs to generate the MIDI file from a dataset. For example,
378 Lilypond²⁵ is a music engraving program that can also produce a MIDI file that is playable in a
379 MIDI-capable synthesizer. You also get a beautiful score of the piece as a bonus. Similar to the
380 JythonMusic workflow, the data file was opened in Python, the data was scaled to pitches and those
381 pitches were written in Lilypond syntax to a Lilypond-readable text file. An example of a score is
382 shown in Figure 9. Strong spectral lines can be seen in measures 31 and 35.

384 Mapping data to variations in pitch may not be the optimum solution for sonifying data. A large
385 value of a dataset may be better represented by changes in the volume, emphasizing the strength of
386 the larger value. We did some experiments on such variations and found that the limited ability of
387 humans to sense changes in loudness and to remember a baseline level of loudness over an entire
388 piece made this less effective at sonifying data. Sonifying the data using a constant pitch with
389 variable loudness also led to annoyance caused by the unchanging pitch.

390 Other examples of sonifying solar data include solar oscillations,^{26,27} solar wind data,²⁸ and an
391 interactive image to music experience.²⁹ The first three examples are for 1-D time series while the
392 fourth uses the motion of a person to sample an image. Others have produced a sonified solar
393 system.³⁰ The image sonifications described herein may be one of the few examples of such a

EUV on 27 Feb 2014 (Solar Maximum)

Piano Old Sol

He II 304 Fe XVI 335

FIG. 9. The first page of a piano score of the EVE spectrum in Figure 2 created by Lilypond. The He II 304 Å line can be seen in measure 31 and the Fe XVI 335 Å line in measure 35. The scaling to pitch is different than the sonified example to better fit on the staves.

394 project.

395 VII. CONCLUSIONS

396 We have sonified solar data as time series, an EUV spectrum, a time series of EUV spectral
 397 irradiances, EUV images with various techniques, and a time sequence of EUV images. The EUV
 398 spectrum showed that the independent variable does not have to be time. We demonstrated that
 399 using a Hilbert curve to address a solar image gives a sonification that shows more of the image
 400 variations and less of the shape of the Sun.

401 One shortcoming of the Hilbert curve sampling method is the separation of two regions near the
 402 limb. In these examples, images are sampled by a curve that crosses from the upper left quadrant

403 to the upper right near the equator. This means the northern polar region is sampled in two distinct
404 areas far from one another. The two lower quadrants do not have a direct connection and the
405 southern polar region is also divided into two distinct regions, one at the beginning of the series
406 and the other at the end. This can be remedied by rotating the Hilbert curve (or the image) 90°
407 in either direction, which moves the connection between quadrants to the poles and keeps those
408 regions in a smaller neighborhood while dividing the equatorial limb sectors into disparate parts of
409 the sampling curve.

410 Other techniques can be used to sonify solar images. Coincident images observed in different
411 wavelengths of light can be sampled and placed in different timbres or pan positions. Once the
412 next solar maximum passes, another EVE spectrum could be used to play against the solar maxi-
413 mum spectrum illustrated here. Higher-order Hilbert curves can be constructed to sample a series
414 of images. This would keep points within a neighborhood in both space and time. **Software that**
415 **directly produces sounds rather than adhering to the MIDI standard might create sonifica-**
416 **tions that better represented the data. This could overcome the limited number of pitches**
417 **available in the MIDI standard.**

418 Sonifying solar images is a way to explore the interface between tempo and pitch. Increasing
419 the tempo to 3000 bpm (or 50 Hz) allows you to investigate whether an extremely rapid tempo
420 results in an envelope with the individual pitches providing an amplitude modulation of that enve-
421 lope. Frequencies of 15–30 Hz (900–1800 bpm) are near the limit of pitch discrimination.³¹ The
422 difference between the buzz saw of the raster scan image (Sec. III C) and the smoother sound of
423 Hilbert curve sampling of Sec. V is one example of how the envelope makes a big difference in the
424 perception of the data.

425 Listening to the Sun allows people to enjoy our closest star in a new direction. This does not
426 apply only to the blind, most people can hear the variations of the Sun. With time these techniques
427 will also allow people to more fully explore images as well.

428 VIII. QUESTIONS AND OTHER PROJECTS

429 Here are some ideas that can motivate students to listen to their data:

- 430 1. Can you find ways to vary the **tempo of the music to represent variations in a data set?**

431 Scientific data tends to have even spacing and the simplest way to sonify the data is to
432 maintain an even tempo. You can use the JythonMusic routine `Mod.tie.Pitches` to tie together
433 identical notes to add some variety to the rhythmic spacing. Another routine, `Mod.accent`
434 allows you to accent a beat, which also provides some texture to the music.

- 435 2. Can loudness be used to emphasize important features in a log-scaled variable? Comparing
436 the score of the spectrum in Figure 9 with the physical data in Figure 2, we can see that a
437 few emission lines outshine much of that spectral region but that dominance is not reflected
438 in the sonification. Perhaps increasing the loudness of the strong emission lines would better
439 illustrate this dominance.
- 440 3. Three-color AIA images are created by putting coincident images in different wavelengths
441 into individual color channels. These can be sonified by assigning a voice and pan position
442 to each of the channels that will audibly emphasize the differences in the channels.
- 443 4. A wavelet analysis of a time series can be used to isolate persistent from ephemeral frequen-
444 cies. Can a wavelet spectrum be sonified to show the persistent frequencies as droning notes
445 and ephemeral events as more rapid variations?
- 446 5. Can other instruments be played against the synthesizer output? The sonified data has no
447 explicit key, so improvised solos and rhythms can be played along with the sonified data.

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449 Version 4.6 of the JythonMusic software was downloaded from <https://jythonmusic.me>. All of
450 the data used in this research is available as continually updated files from publicly-accessible sites.
451 The monthly averaged (`SN_m_tot_V2.0.csv`) and the annually averaged (`SN_y_tot_V2.0.csv`) In-
452 ternational Sunspot Number (Version 2) data were obtained from the Solar Influences Data Cen-
453 ter (<http://sidc.oma.be/silso/datafiles>). Daily averaged SEE measurements were obtained as the
454 SEE Level 3 Merged NetCDF file at http://lasp.colorado.edu/data/timed_see/level3/latest_
455 `see_L3_merged.ncdf`. Daily averaged EVE measurements were obtained the EVE Level 3 Merged
456 NetCDF file at [http://lasp.colorado.edu/eve/data_](http://lasp.colorado.edu/eve/data_access/evewebdataproducts/merged/EVE_)
`access/evewebdataproducts/merged/EVE_`

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