

# Plasma Motions and Turbulent Magnetic Diffusivity of Active Region AR 12158 Using a Minimum Energy Functional and Non-Force-Free Reconstructions of Vector Magnetograms

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**Abstract** We present a generalization of the resistive minimum-energy fit (MEF-R: Tremblay and Vincent in *Solar Phys.* **290**, 437, 2015) for non-force-free (NFF) magnetic fields. In MEF-R, an extremum principle is used to infer two-dimensional maps of plasma motions  $[v(x, y)]$  and magnetic eddy diffusivity  $[\eta_{\text{eddy}}(x, y)]$  at the photosphere. These reconstructions could be used as boundary conditions in data-driven simulations or in data assimilation. The algorithm is validated using the analytical model of a resistive expanding spheromak by Rakowski, Laming, and Lyutikov (*Astrophys. J.* **730**, 30, 2011). We study the flaring Active Region AR 12158 using a series of magnetograms and Dopplergrams provided by the *Helioseismic and Magnetic Imager* (HMI) onboard the *Solar Dynamics Observatory* (SDO). The results are discussed for a non-force-free magnetic-field reconstruction  $[B_{\text{NFF}}]$  (Hu and Dasgupta in *Solar Phys.* **247**, 87, 2008). We found that the vertical plasma velocities  $[v_z(x, y)]$  inferred using MEF-R are very similar to the observed Doppler velocities  $[v_r(x, y)]$ . Finally, we study the potential spatial correlation between microturbulent velocities and significant values of  $\eta_{\text{eddy}}(x, y)$ .

**Keywords** Magnetic fields, photosphere · Velocity fields, photosphere · Active regions · Granulation

## 1. Introduction

Observations of plasma proper motions  $[v(x, y)]$  are limited to the line-of-sight component, *e.g.* the Doppler velocity  $[v_r(x, y)]$ . Numerous methods have been devised to reconstruct transverse (or horizontal in approximation) plasma motions  $[v_h(x, y)]$  at the photosphere from vector magnetograms (*e.g.* Welsch *et al.*, 2007). They are based on simplified

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